

12th to 14th September 2022



A study of SWIM directional wave spectra during rogue wave cases

DALPHINET Alice¹, AOUF Lotfi¹, LE MERLE Eva², HAUSER Danièle³

¹ Météo-France ² ISMAR ³ LATMOS

13/09/22

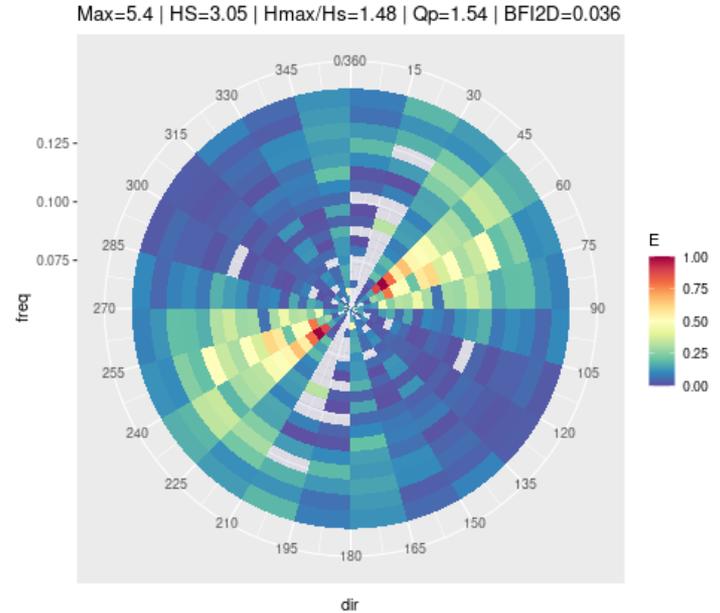
3rd CFOSAT International Science team meeting



Context

- SWIM measures 2D wave spectra on 70x90 km boxes, with a good quality from 0,056 Hz to 0,16Hz
- Spectral resolution of 24 directions (ambiguity) and 32 frequencies
- Possibility to compute characteristics of wave spectra and index of extrem waves (peakedness, BFI, r)

- Is there any correlation between SWIM spectra and rogue waves observations ?

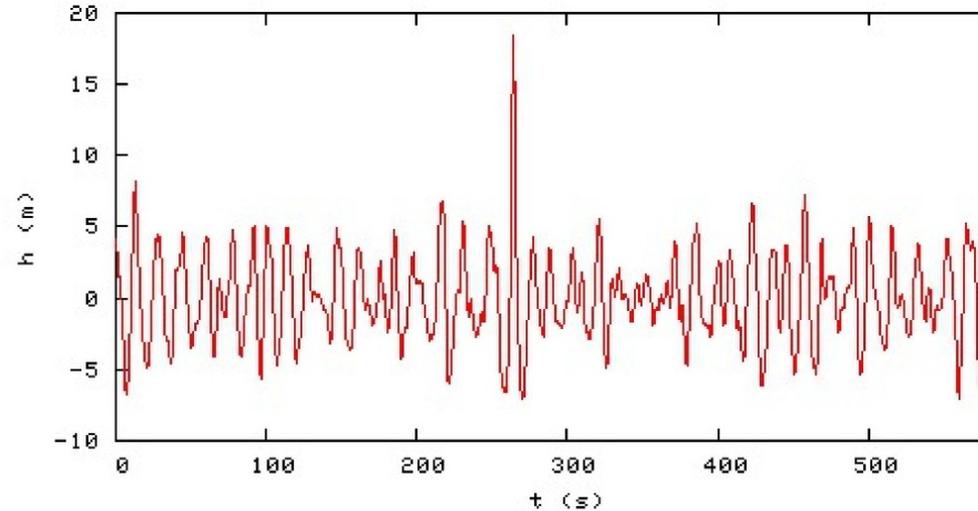


*Example of SWIM height spectrum in frequency
The 02/01/2020 23:10 in Naturaliste Cape
(Australia)*



Observation of rogue waves

- Use of the CMEMS in-situ buoys network.
 - Selection of buoys measuring maximum wave height.
- a rogue wave corresponds to $H_{max}/SWH > 2$



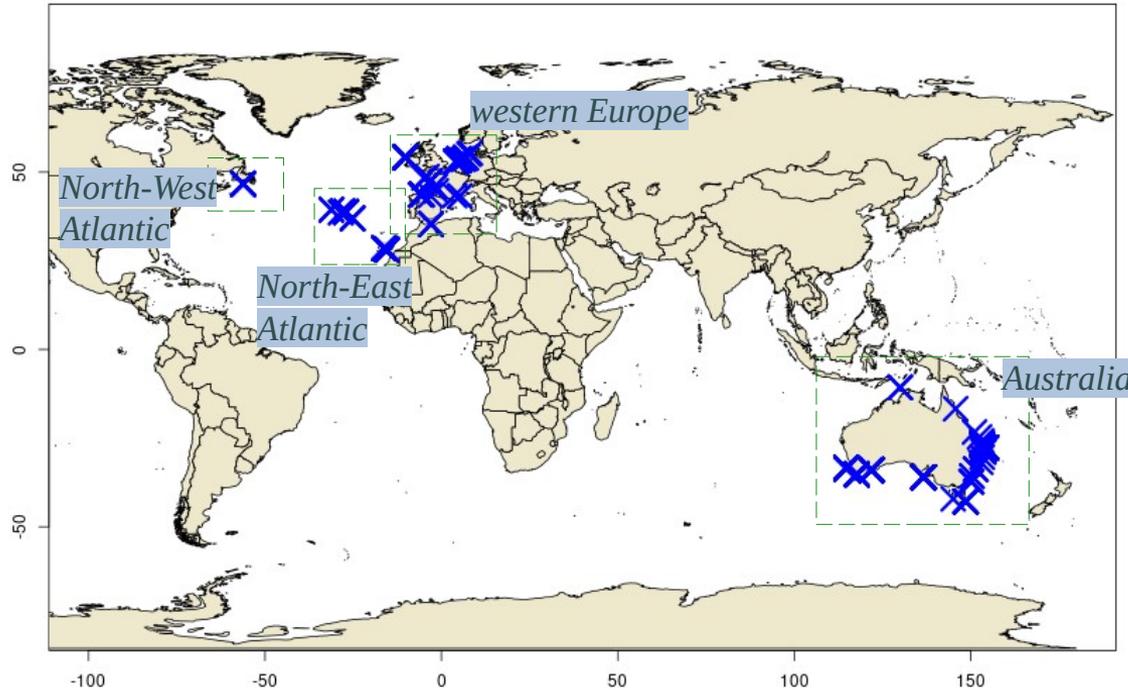
The 1995 Draupner wave

- Colocalisation at $0,5^\circ$ of distance and 90 min in time.
 - Selection of cases with $SWH > 50$ cm and $PP > 8$ s
- range of good SWIM data quality
- Filtering of spectra with less than 30% of missing bins



Observation of rogue waves

- From January 2020 to July 2022 : 475 colocalisations

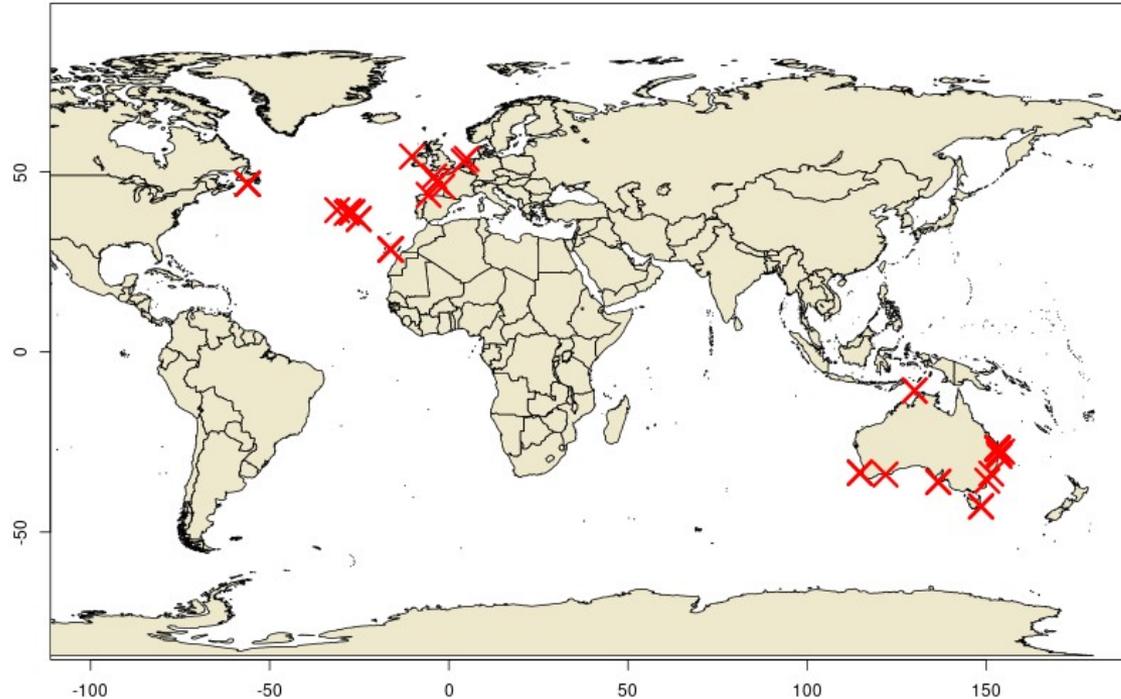


*Selection from the in-situ TAC
of Copernicus Marine Service*



Observation of rogue waves

- From January 2020 to July 2022 : 48 cases of rogue waves



*Selection from the in-situ TAC
of Copernicus Marine Service*

Outline

- Computation of spectral indexes on the whole period
- 2022/01/01 Case of swell near french coast
- 2021/08/09 Case of storm near Australia



Container ship after a storm in Pacific in December 2020

Computation of spectral indexes

- Spectral peakedness thanks to Goda parameter

$$Qp = \frac{2 \sum_{f_{\min}}^{f_{\max}} f F^2(f) df}{\left[\sum_{f_{\min}}^{f_{\max}} F(f) df \right]^2}$$

Goda, 1976

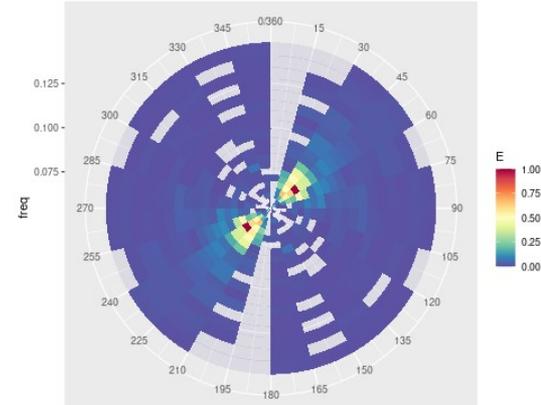
- Benjamin Fair index : indicator of non-linearities of wave interactions and probability of occurrence of extreme waves in the case of unidirectional seas

$$BFI = k_0 \sqrt{m_0} Qp \sqrt{2\pi}$$

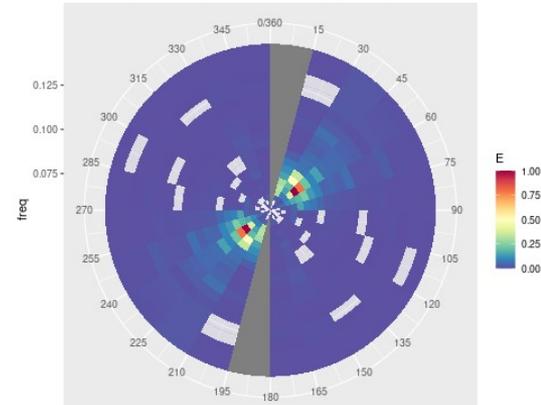
Mori et al, 2011

k_0 : mean wavenumber
 m_0 : 0th order moment of
the energy of the spectrum

Max=14.9 | HS=2.53 | Hmax/Hs=1.44 | Qp=3.11 | BFI2D=0.035



Max=37.6 | HS=2.53 | Hmax/Hs=1.44 | Qp=3.99 | BFI2D=0.044



Computation of spectral indexes

- Spectral peakedness thanks to Goda parameter

$$Qp = \frac{2 \sum_{f_{\min}}^{f_{\max}} f F^2(f) df}{\left[\sum_{f_{\min}}^{f_{\max}} F(f) df \right]^2}$$

Goda, 1976

- Benjamin Fair index : indicator of non-linearities of wave interactions and probability of occurrence of extreme waves in the case of unidirectional

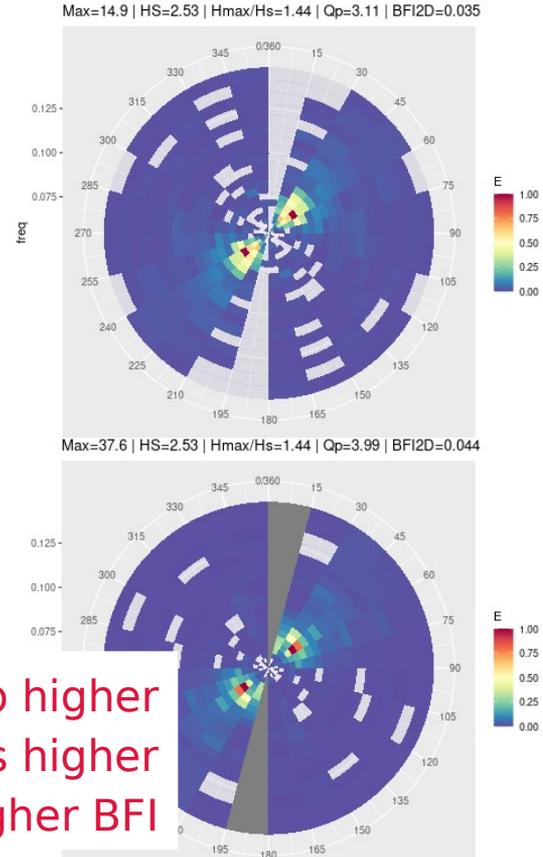
Higher the steepness, higher the BFI

$$BFI = k_0 \sqrt{m_0} Qp \sqrt{2\pi}$$

Mori et al, 2011

k_0 : mean wavenum
 m_0 : 0th order mom
the energy of the sp

Qp higher
steepness higher
=> higher BFI



Computation of spectral indexes

- Directional spread (a_1/b_1 Fourier coefficients)

$$\sigma_\phi(f) = \sqrt{2 \times \left(1 - \sqrt{a_1(f)^2 + b_1(f)^2} \right)}$$

- Benjamin Fair index 2D : inclusion of directional effects

$$BFI_{2D} = \frac{BFI}{\sqrt{1 + \alpha_2 R}}$$

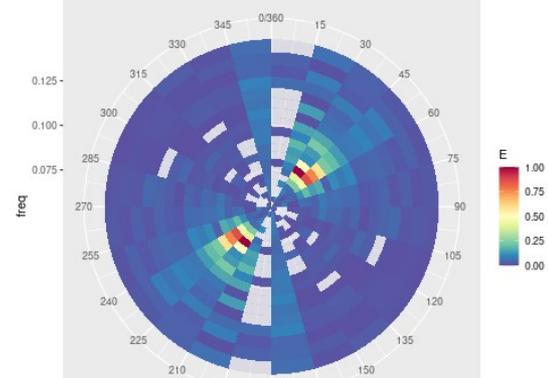
$$R = \frac{1}{2} \sigma_\phi^2 \pi Q p^2$$

Mori et al, 2011

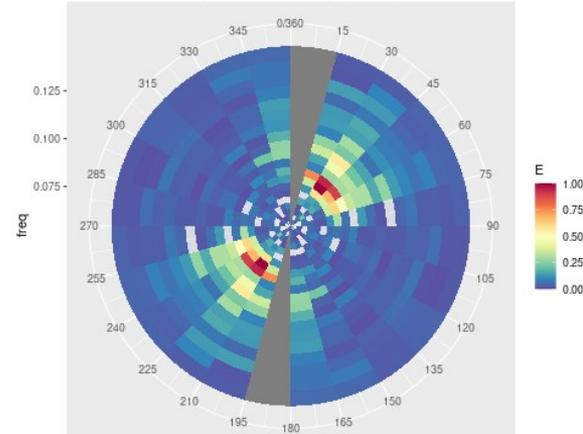
Study of spectral indexes on SWIM spectral data :

Le Merle et al, 2021

Max=9.1 | HS=2.8 | Hmax/Hs=1.68 | Qp=1.97 | BFI2D=0.041



Max=8.2 | HS=2.8 | Hmax/Hs=1.68 | Qp=2.23 | BFI2D=0.032



Computation of spectral indexes

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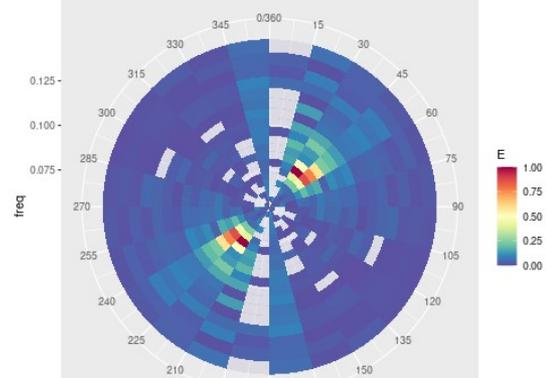
Mori et al, 2011

Smaller the directional spread, higher the BFI

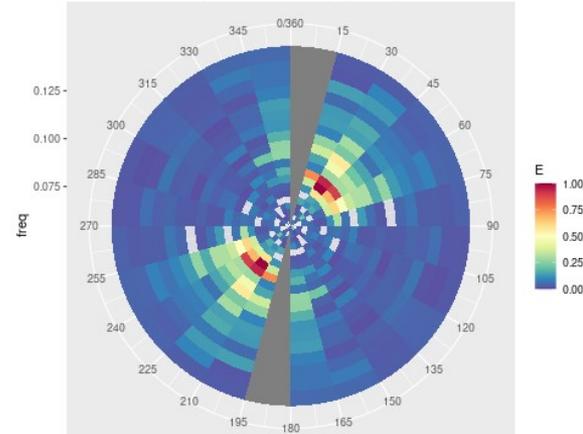
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Computation of spectral indexes

- Crest-trough correlation r calculated from the spectrum :
Auto-correlation of the sea surface elevation at half the wave period.

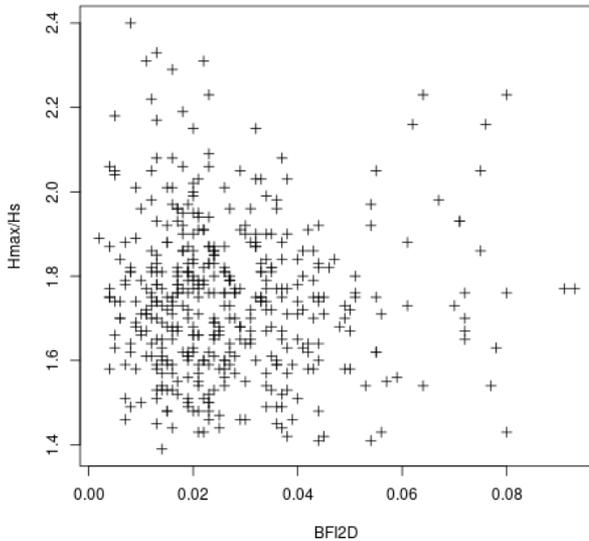
$$r = \frac{1}{m_0} \sqrt{\rho^2 + \lambda^2}, \text{ where } \rho = \int_0^{\infty} S(f) \cos(2\pi f \tau) df \text{ and } \lambda = \int_0^{\infty} S(f) \sin(2\pi f \tau) df,$$

where $\tau = \frac{\bar{T}}{2}$ is the lag time at half the spectral mean period $\bar{T} = \frac{m_0}{m_1}$.

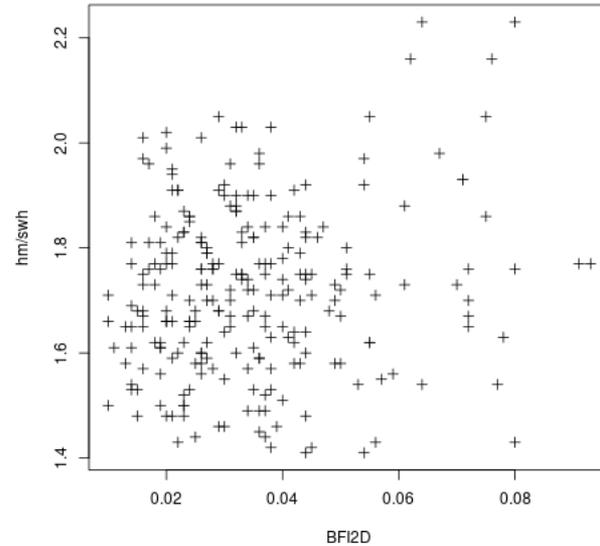


BFI2D

- No correlation between BFI2D of SWIM data and H_{max}/H_s , even for $SWH > 2m$



Cases with $SWH > 1 m$

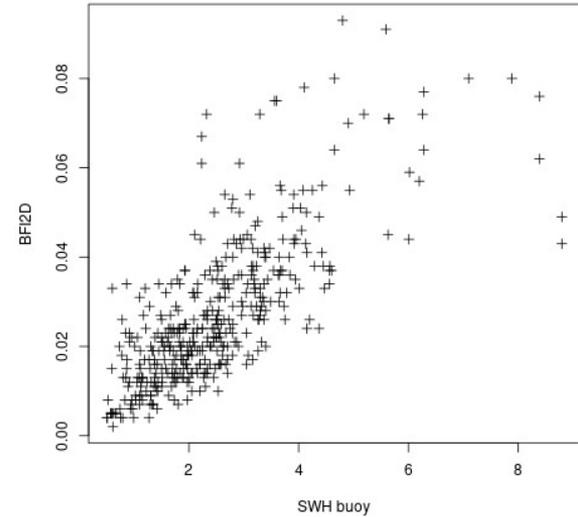


Cases with $SWH > 2 m$

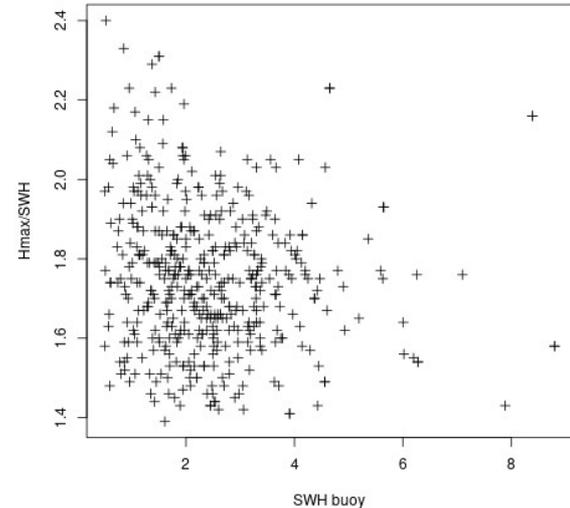


BFI2D

- Graphics of BFI2D function of SWH
 - BFI2D higher with SWH



- Graphics of Hmax/SWH function of SWH
 - A lot of rogue waves with SWH < 2 m



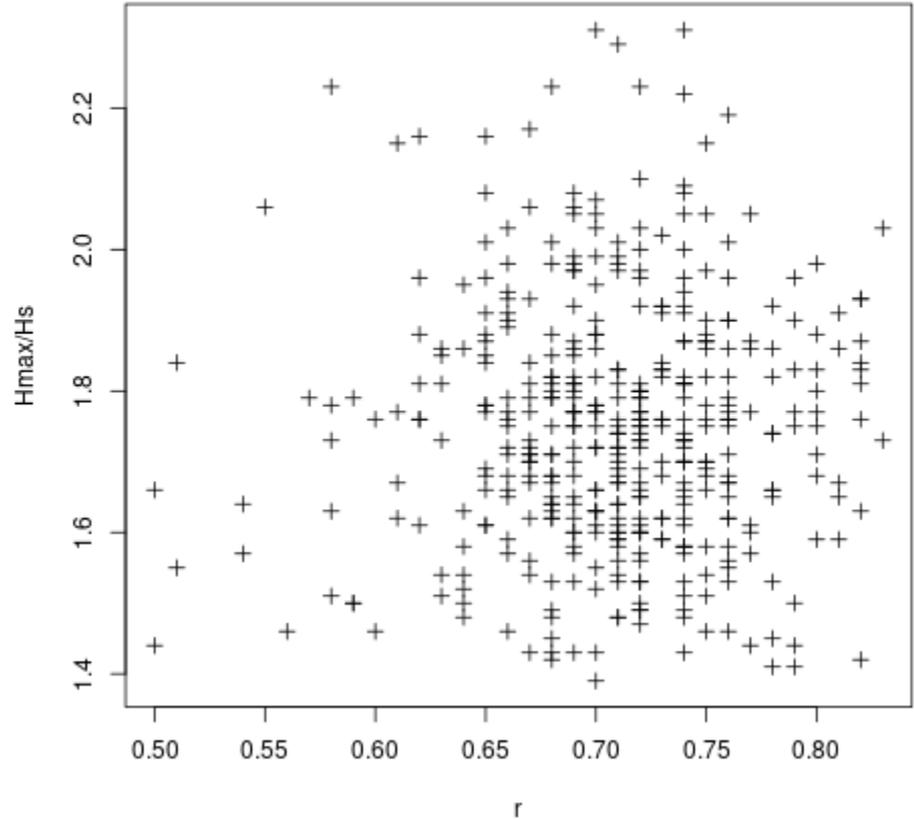
=> We can expect a bad correlation between BFI2D and Hmax/SWH



r correlation

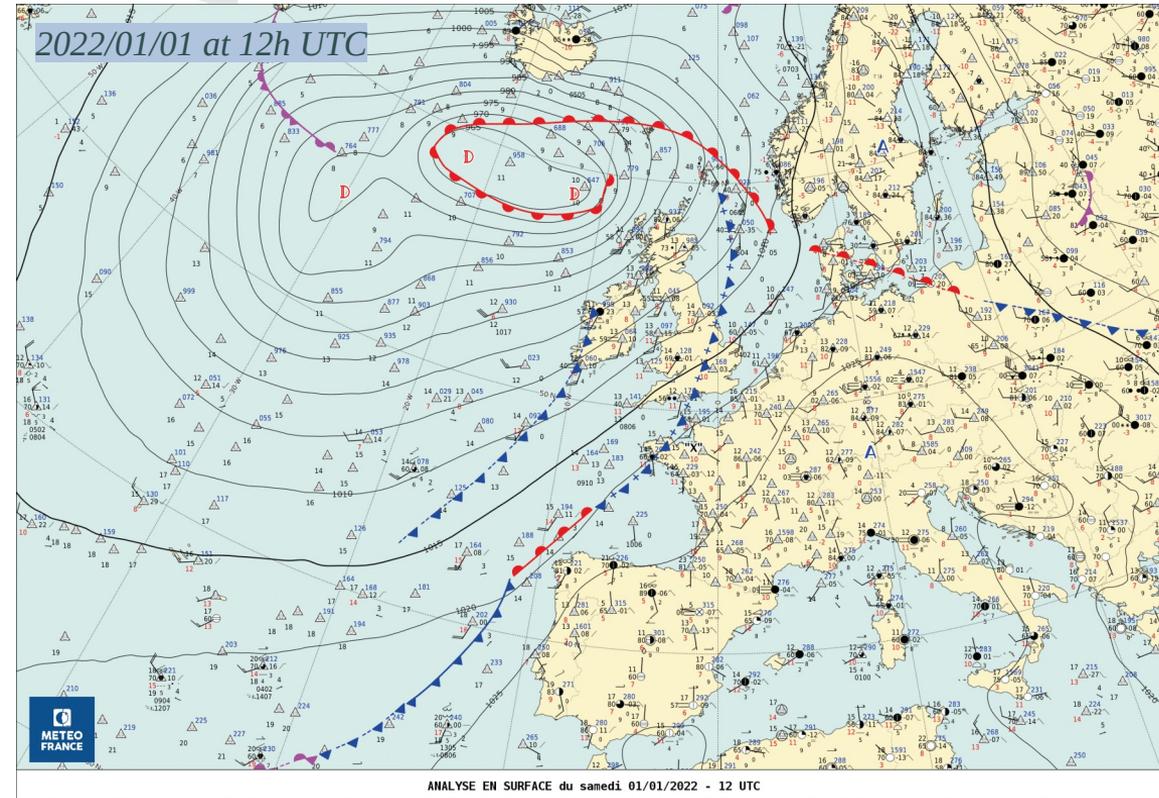
- No correlation between r of SWIM data and H_{max}/H_s

Cases with SWH > 1 m



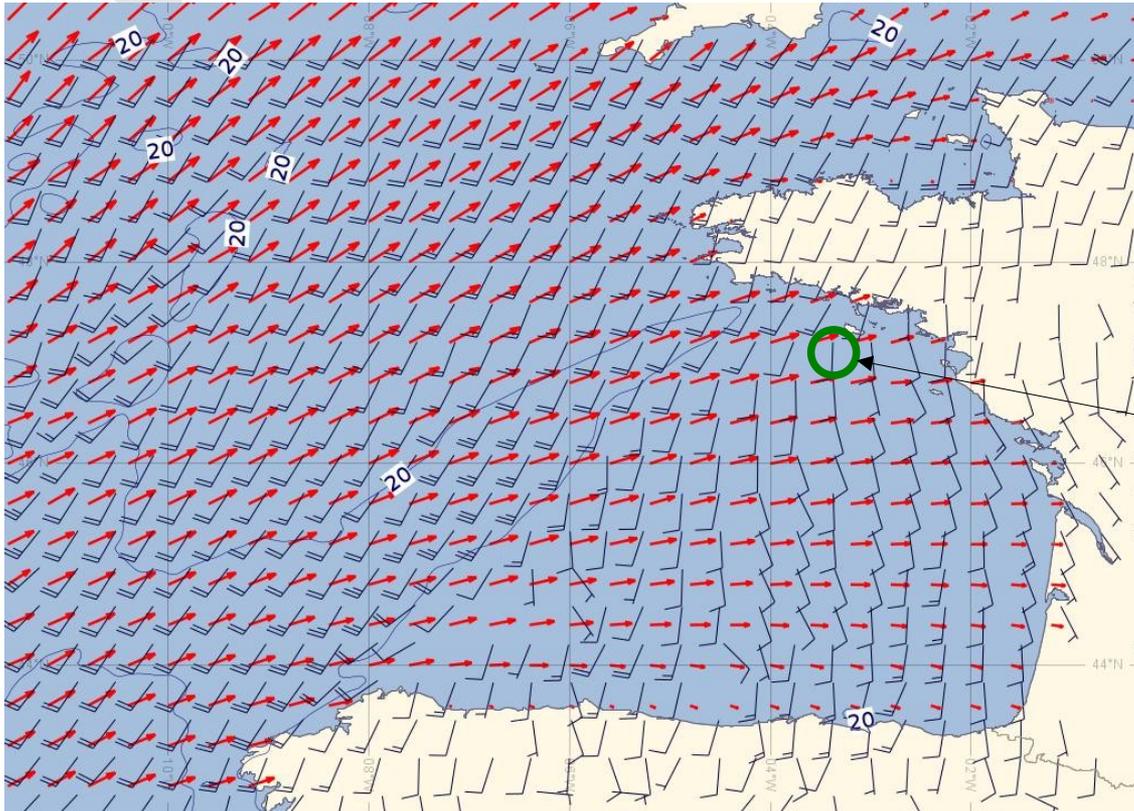
01/01/2022 Case of swell on french coast

2022/01/01 at 12h UTC



- A cold front comes from Atlantic
- It is preceded by a westerly swell of 3,3 m and 12 s

01/01/2022 Case of swell on french coast



- A cold front is coming from Atlantic
- It is preceded by a westerly swell of 3,3 m and 12 s

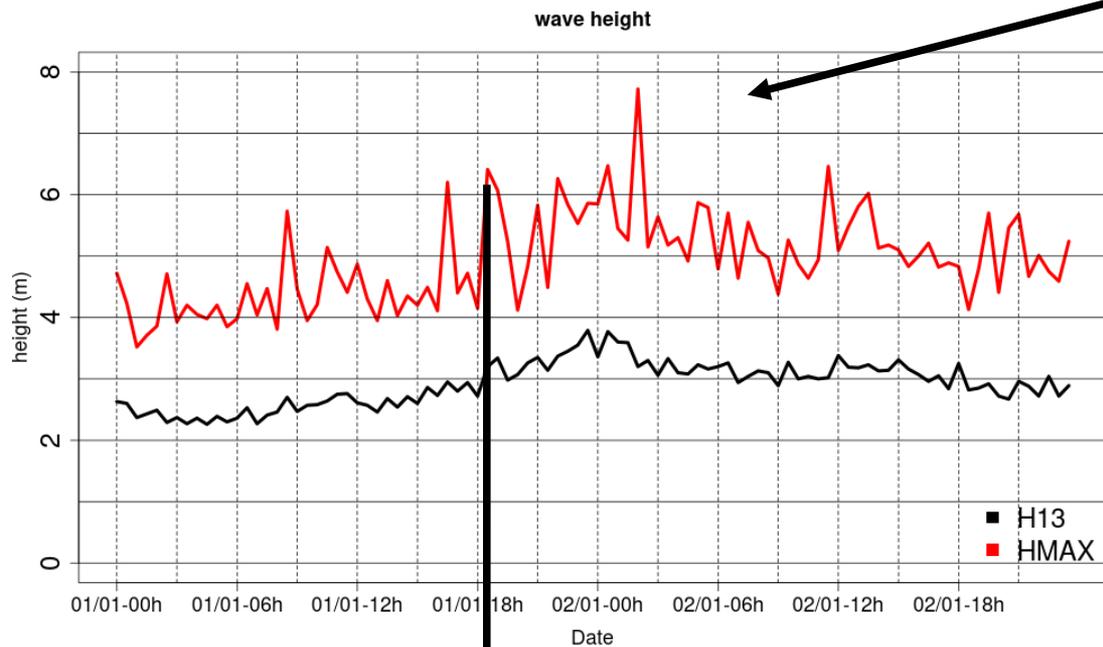
SWIM and buoy observation

2022/01/01 at 18h UTC

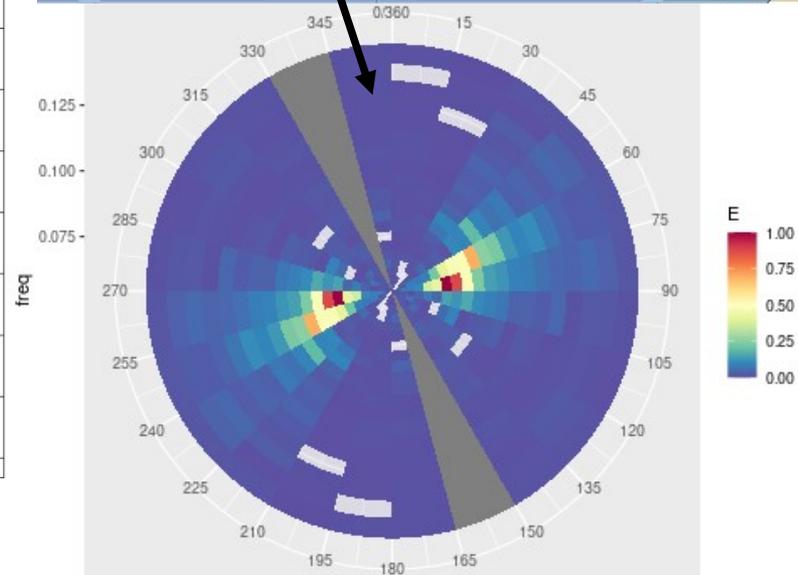
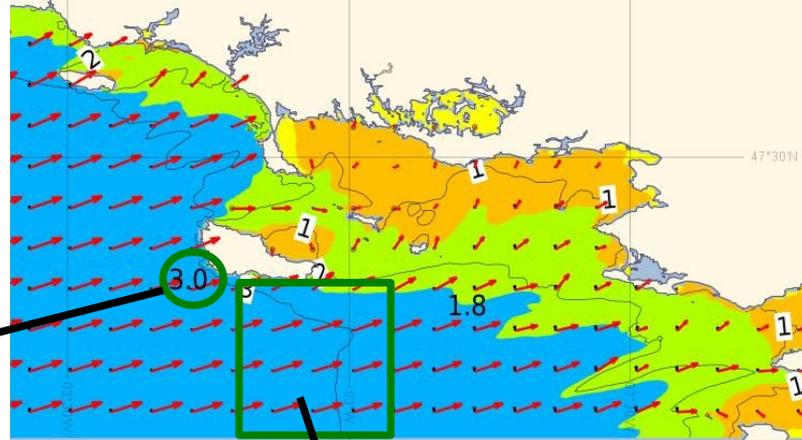
10 m wind in blue from IFS

MFWAM swell in red

Buoy and SWIM observation

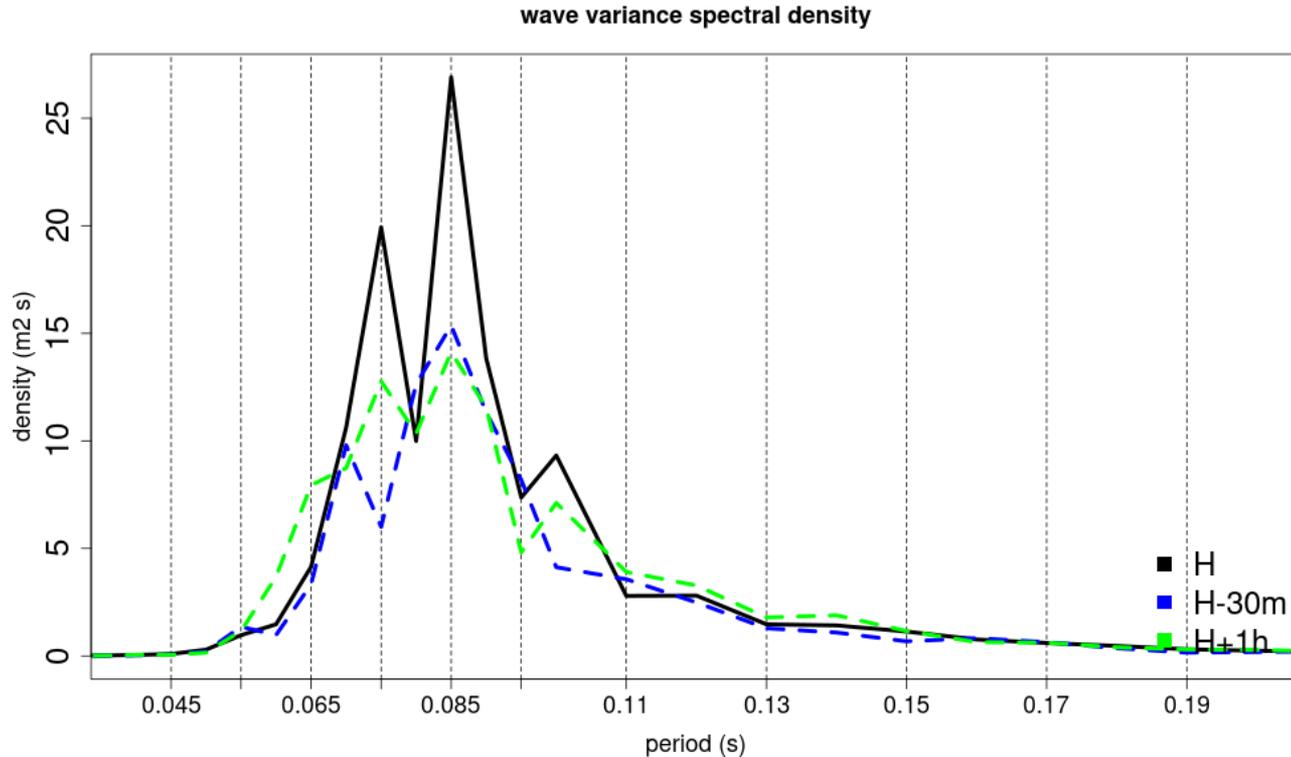


SWH of 3,1 m and Hmax of 6,4 m



2022/01/01 at 18h43 UTC

Spectral specificities according to buoy

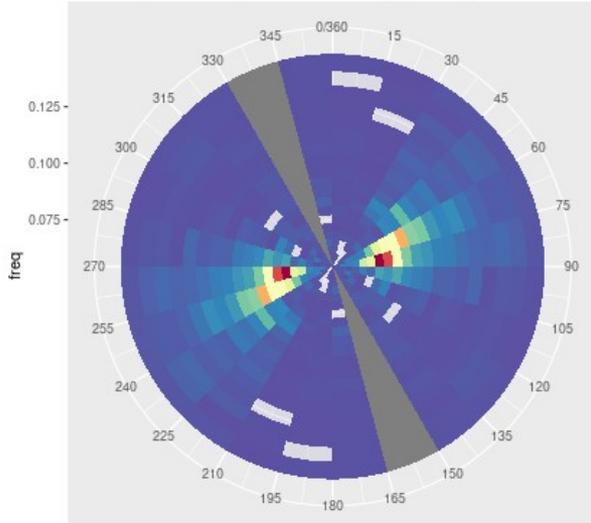


- 2 narrow peaks of energy with close frequencies (period : 11,8 s and 13,3s)
- Just before and after the event, the peakedness of each maximum is much smaller

1D spectra at 18h30 2022/01/01 and adjacent time steps at Belle-Ile buoy

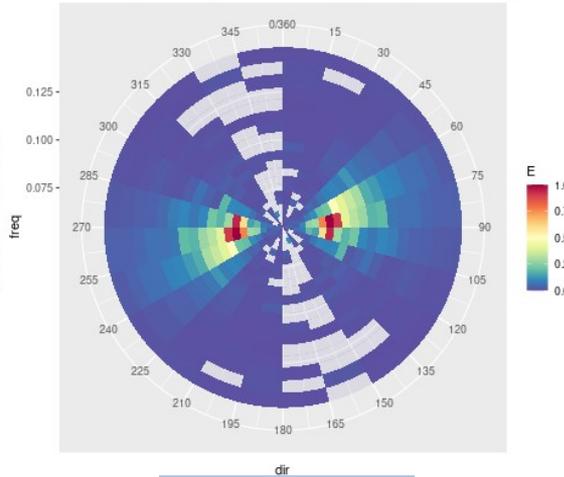
Spectral specificities according to SWIM

Max=7.9 | HS=3.13 | Hmax/Hs=2.05 | Qp=3.08 | BFI2D=0.029 | r=0.5



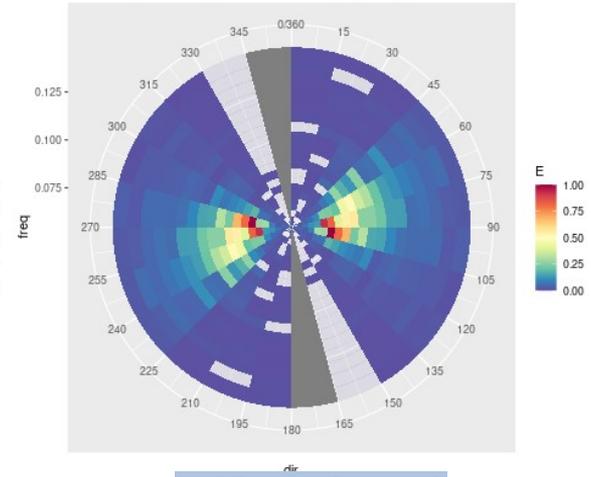
Rogue wave place

Max=11.2 | HS=3.13 | Hmax/Hs=2.05 | Qp=3.32 | BFI2D=0.04 | r=0.52



80 km at the south

Max=8.8 | HS=3.13 | Hmax/Hs=2.05 | Qp=3.1 | BFI2D=0.035 | r=0.51

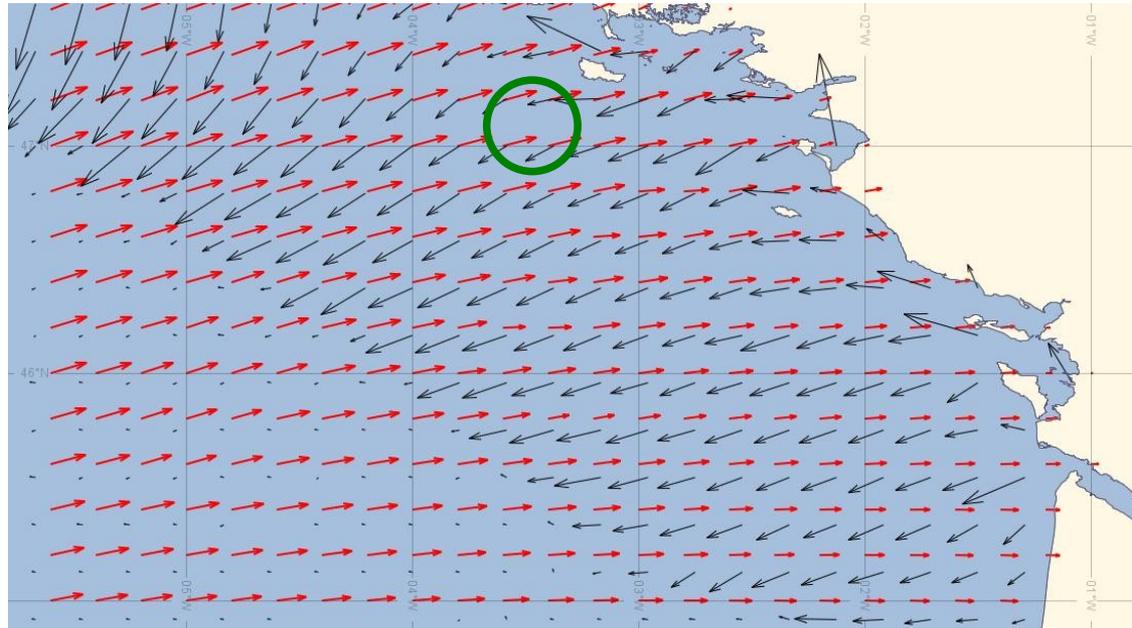


160 km at the south

- 2 peaks at the rogue wave place. 1 peak elsewhere with less variability of energy in frequency and direction space.

Currents impact ?

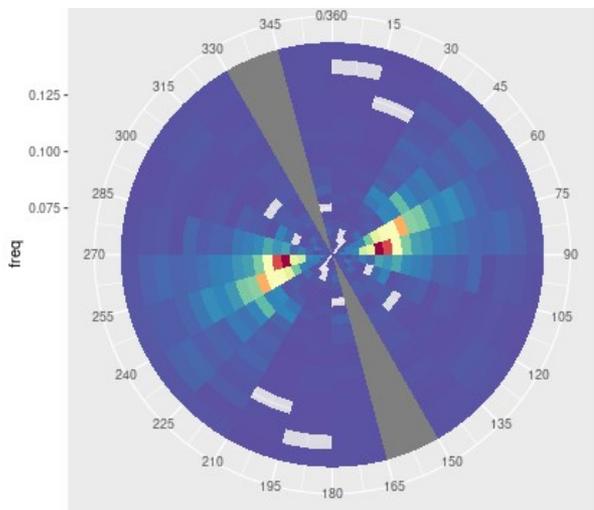
- The rogue wave place occurs exactly at half tide of relatively high tide situation (coef 90)



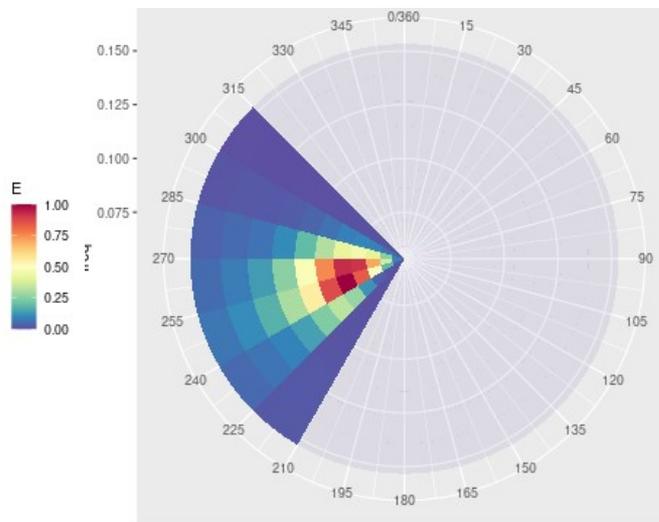
- According to Hycom2D (barotropic model), the currents reach 0,3 m/s (black arrow)
- Slight angle between currents and swell => partial change of direction
- At the south currents and swell are more lined up

2022/01/01 at 18h UTC barotropic currents in black and swell in red

The usefulness of spectral resolution



SWIM



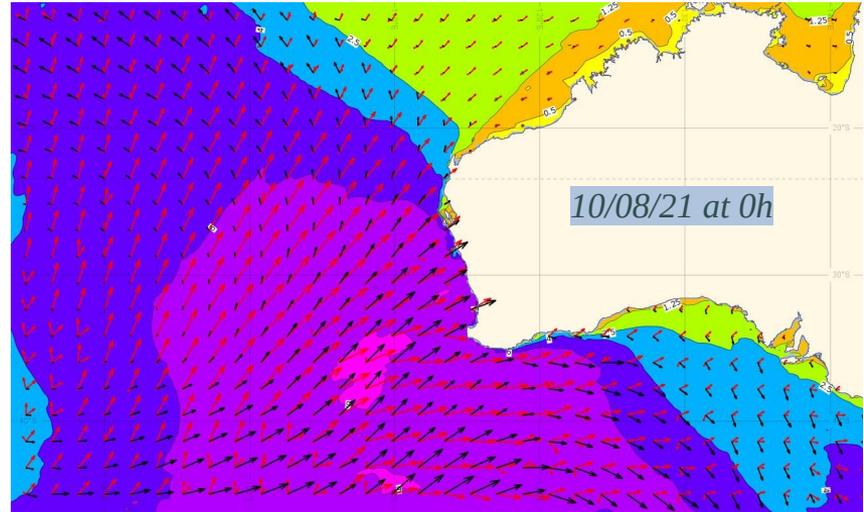
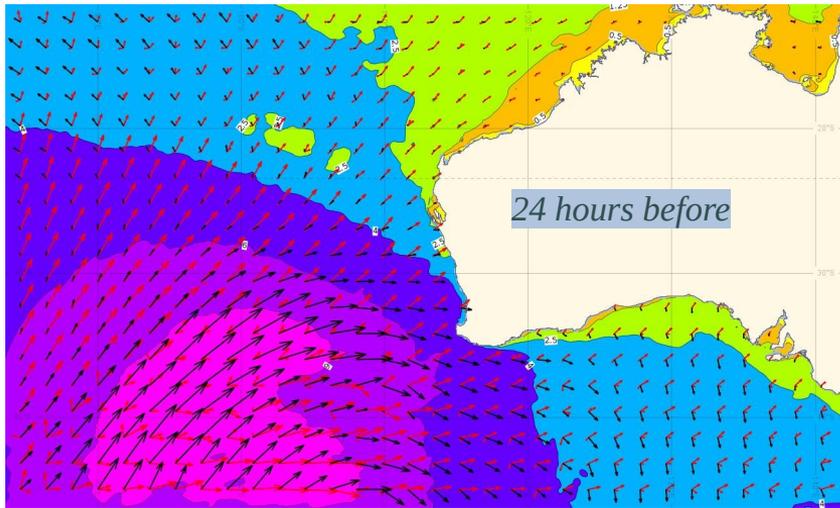
MFWAM

- MFWAM spectrum is smooth with less resolution. It cannot represent 2 peaks of energy.

=> possibility of improvement by a better resolution in direction and frequency

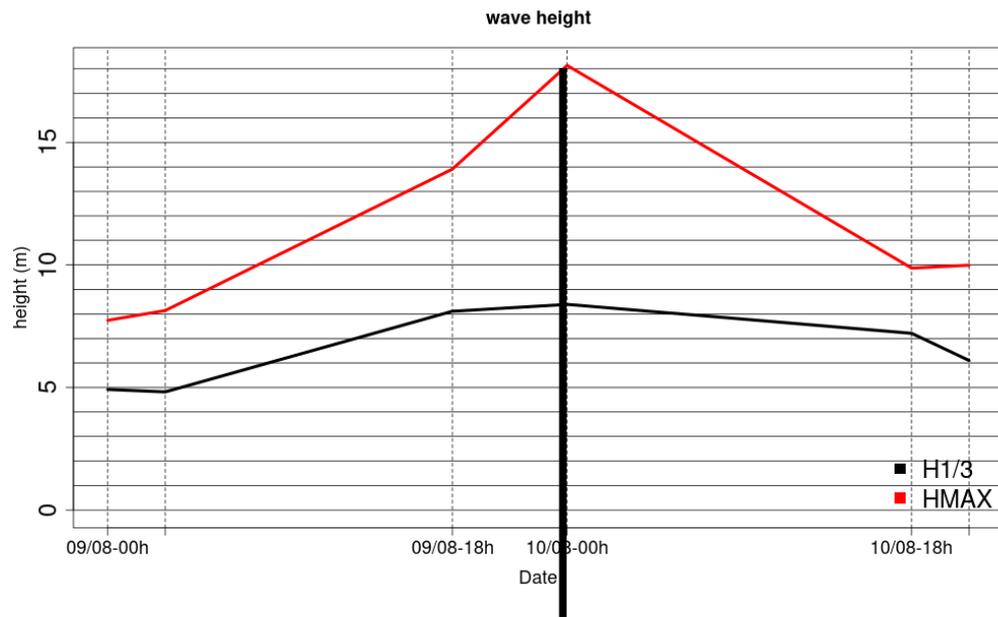
09/08/2021 Case of storm in Australia

MFWAM . Wind sea in black. Swell in red

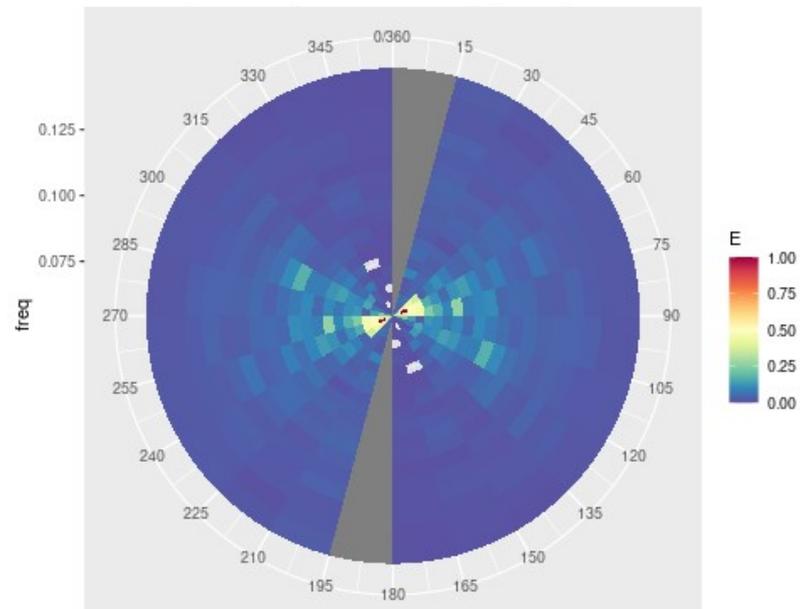


- The model simulates a wind sea of 5,7 m (10,6s), a first swell of 5,1 m and 17,5s.

Buoy and SWIM observation



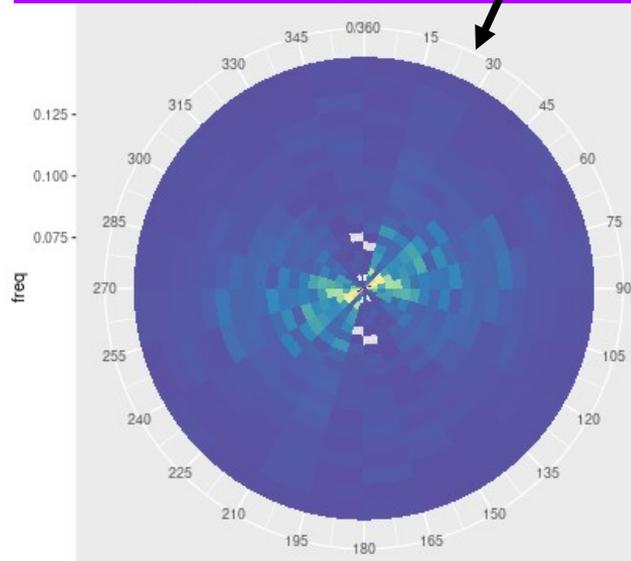
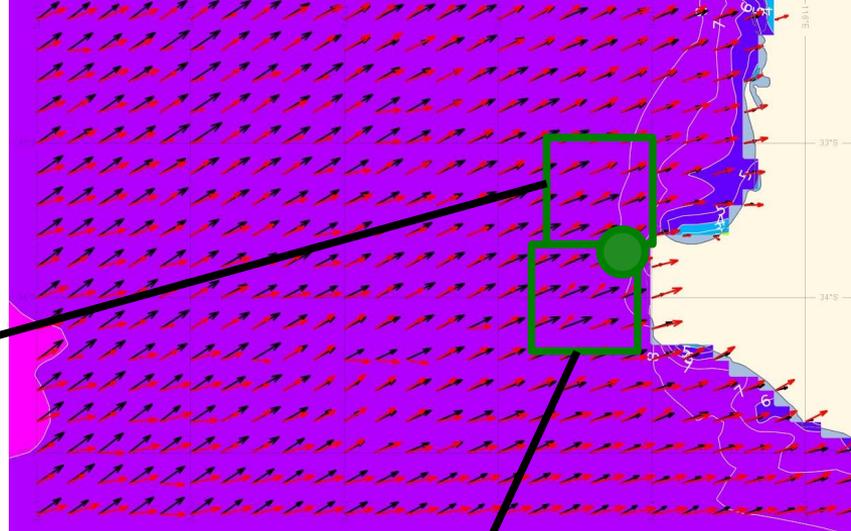
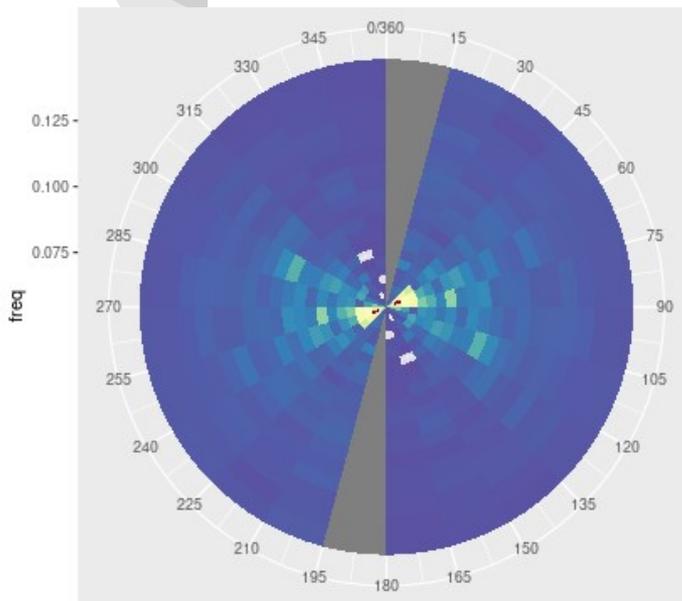
SWH of 8,4 m and Hmax of 18,1 m



2021/08/09 at 23h08 UTC

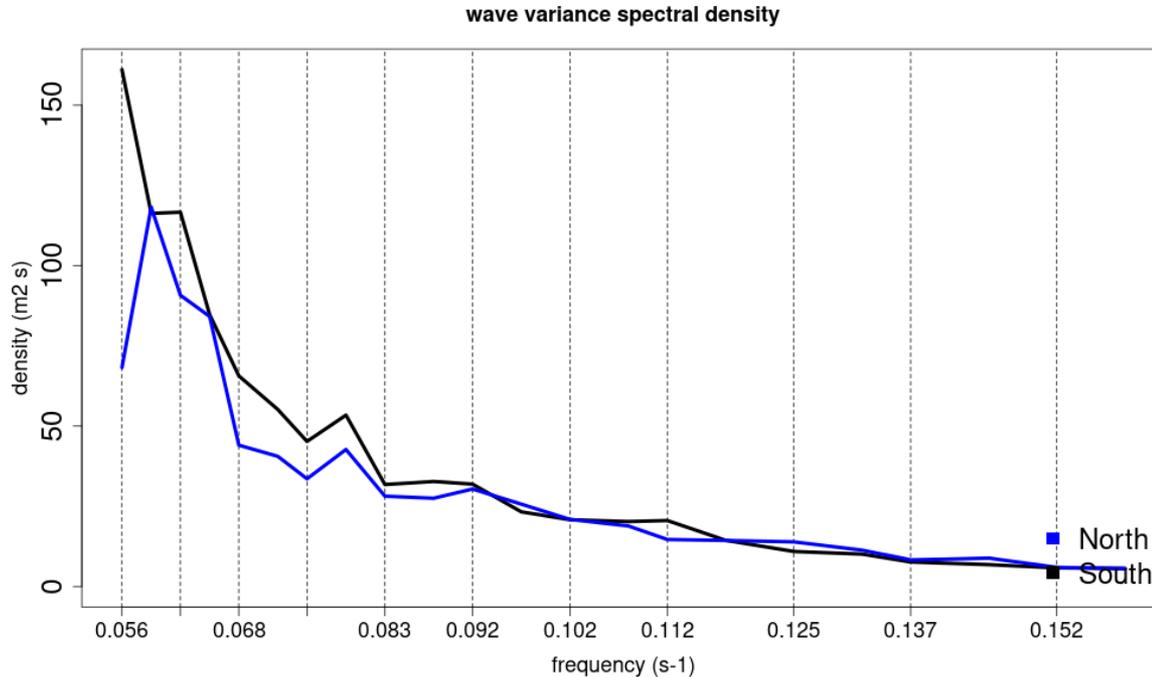
2021/08/09 at 23h08 UTC

SWIM observation



- Narrow peak of energy in low frequency (period 17,5s)
- Unidirectional energy with several frequencies

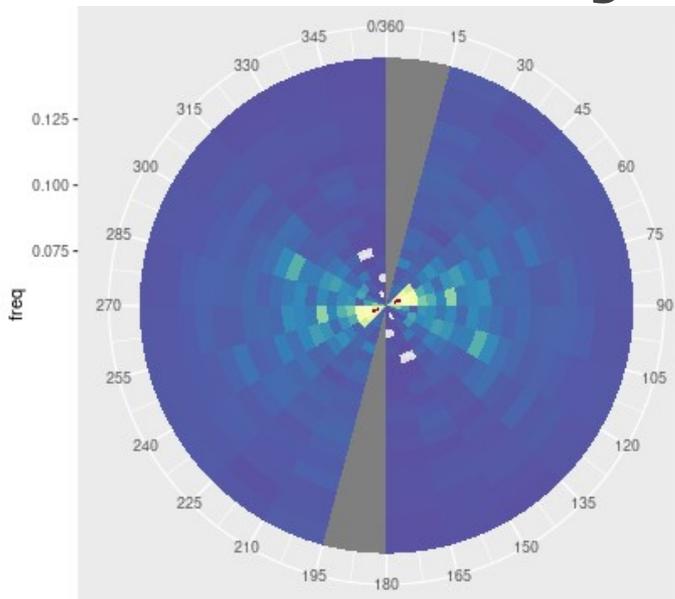
SWIM observation



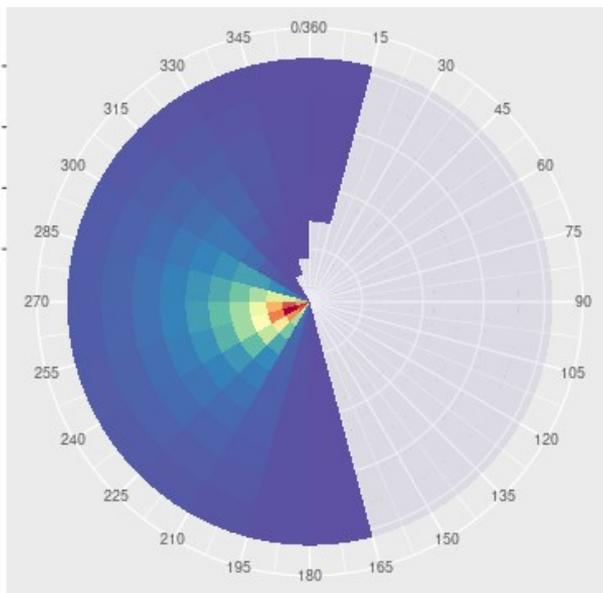
- High peak of energy in low frequency (period 17,5s)
- Energy near the peak at period 16s and 12,5s (wind sea) => possible interactions between waves of close frequencies

1D spectra of SWIM around cape naturalist, the 09/08/21 at 23h

The usefulness of spectral resolution and variability



SWIM



MFWAM

- MFWAM spectrum is smooth with less resolution. Near a Jones shape.



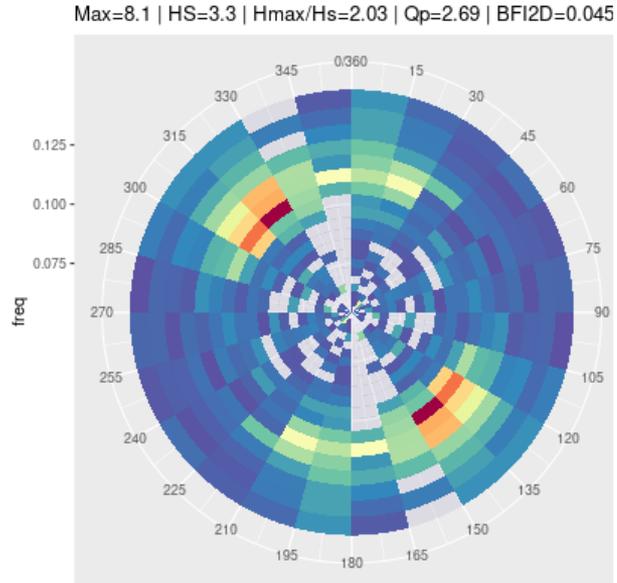
Conclusion

- No obvious relationship between SWIM spectral indexes and rogue waves observations at buoy
- Few rogue waves observations and sometimes too far from buoy in a very variable field
- Spectral indexes from buoy or model may be more correlated with H_{max}/SWH (not studied).



Conclusion

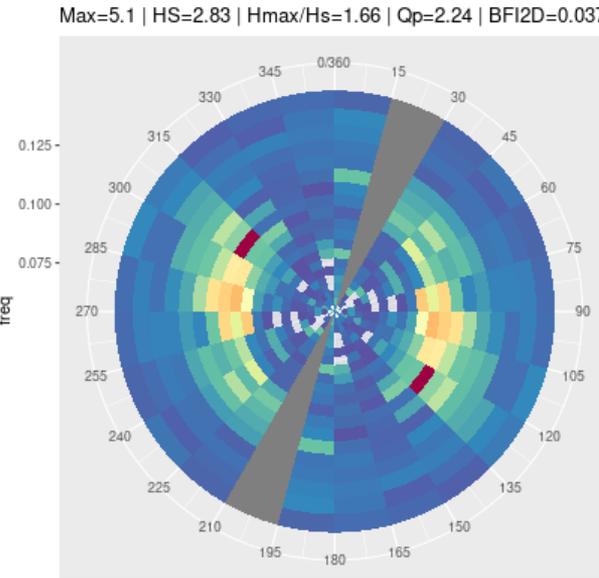
- Some spectra seem to have similar characteristics but correspond to very different H_{max}/H_s



2021/12/17 22:23
Newfoundland
(Atlantic)

SWH of 3,3 m

Hmax of 6,7 m



2020/01/01 08:33
Ireland (Atlantic)

SWH of 2,8 m

Hmax of 4,7 m

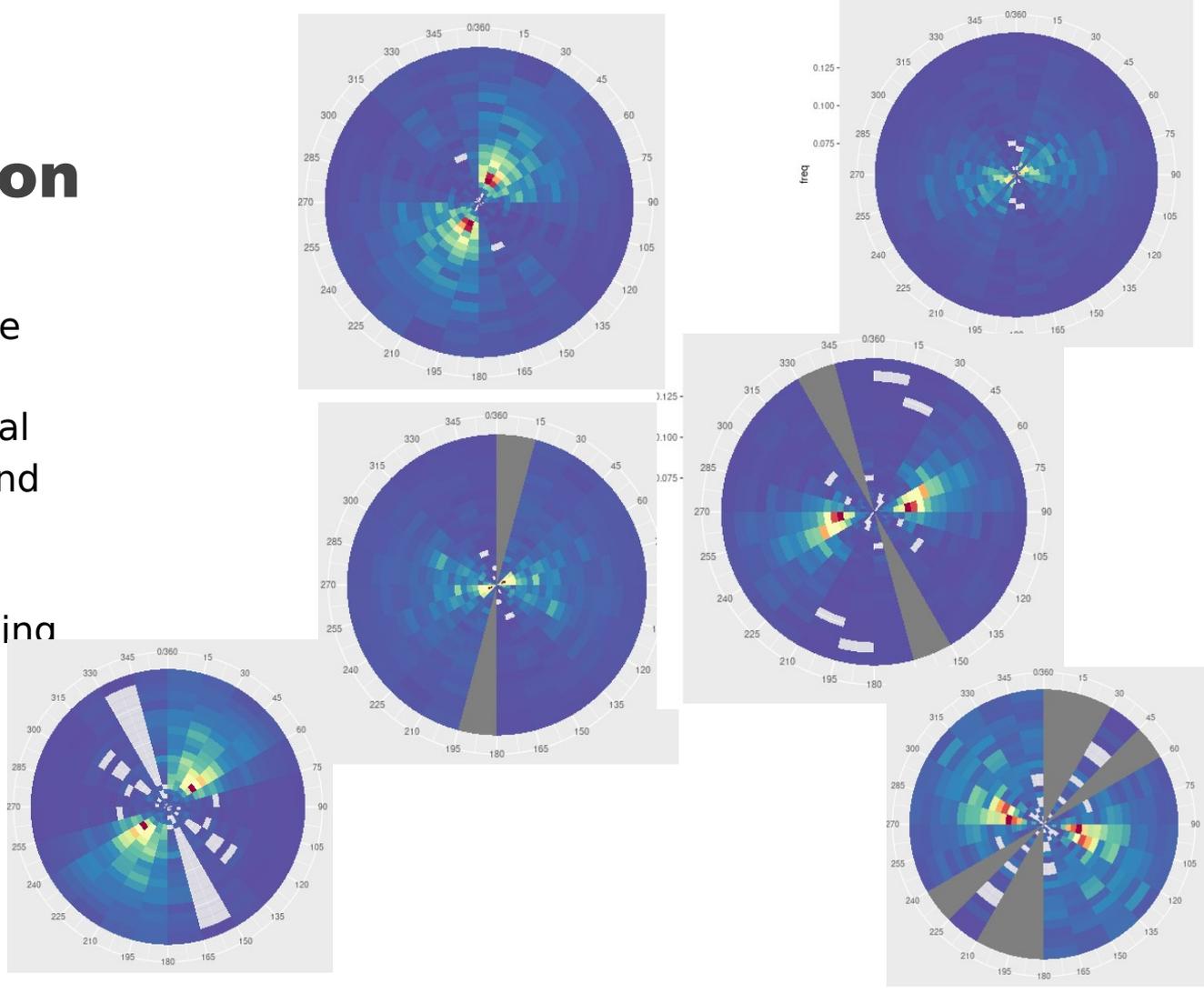


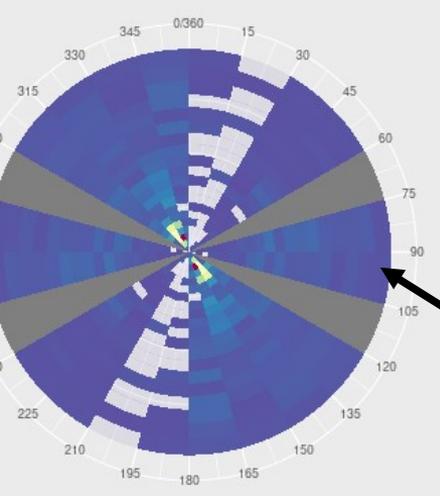
Conclusion

- Some of the rogue wave spectra have a specific narrow and unidirectional shape (case in France and Australia)

=> possible interactions between frequencies explaining rogue waves

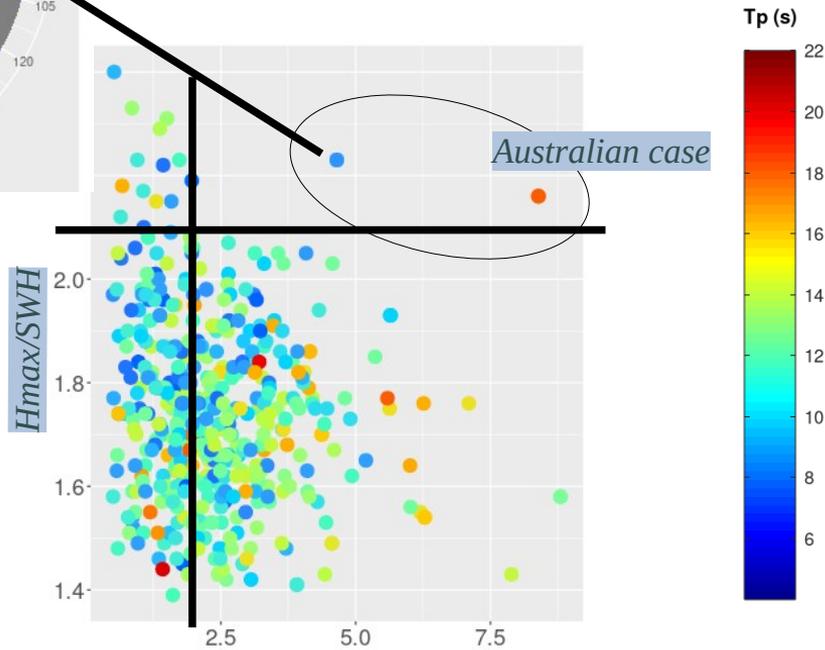
- Capacity of SWIM to represent finely the spectrum





Azores (North Atlantic)
2022/04/10

- If we limit to $swh > 2$ m and $H_{max}/SWH > 2.1$, we get only 2 cases with high BFI2D (0,08)



Statistics over buoys colocalised with SWIM

- With more strict constraints on rogue wave definition and on SWIM quality, encouraging results.
- Too few cases to conclude



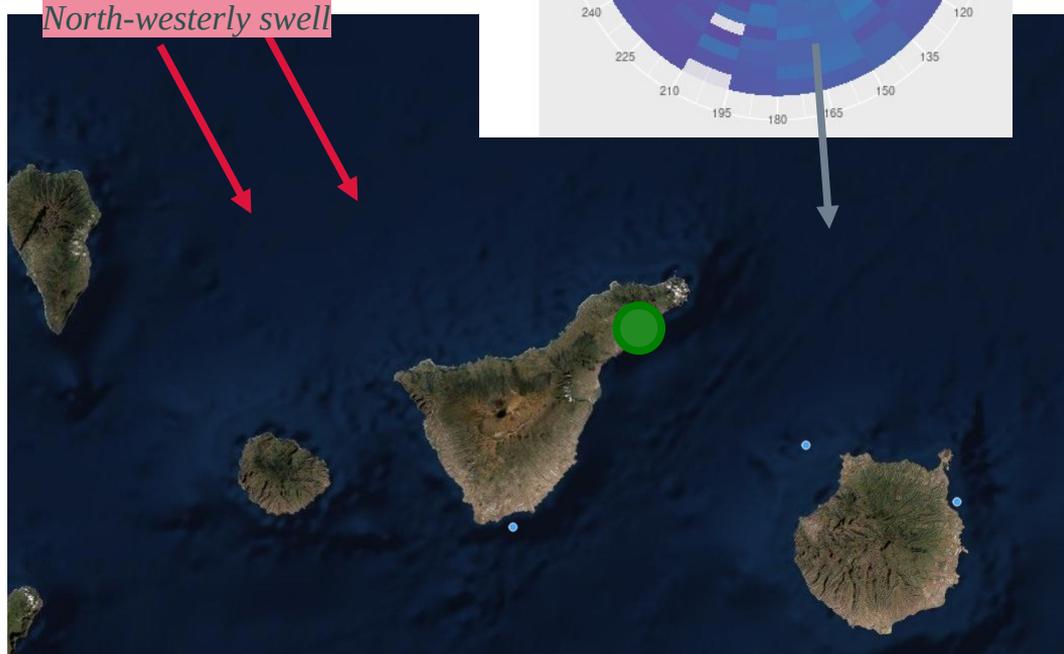
Thank you for your attention



Conclusion

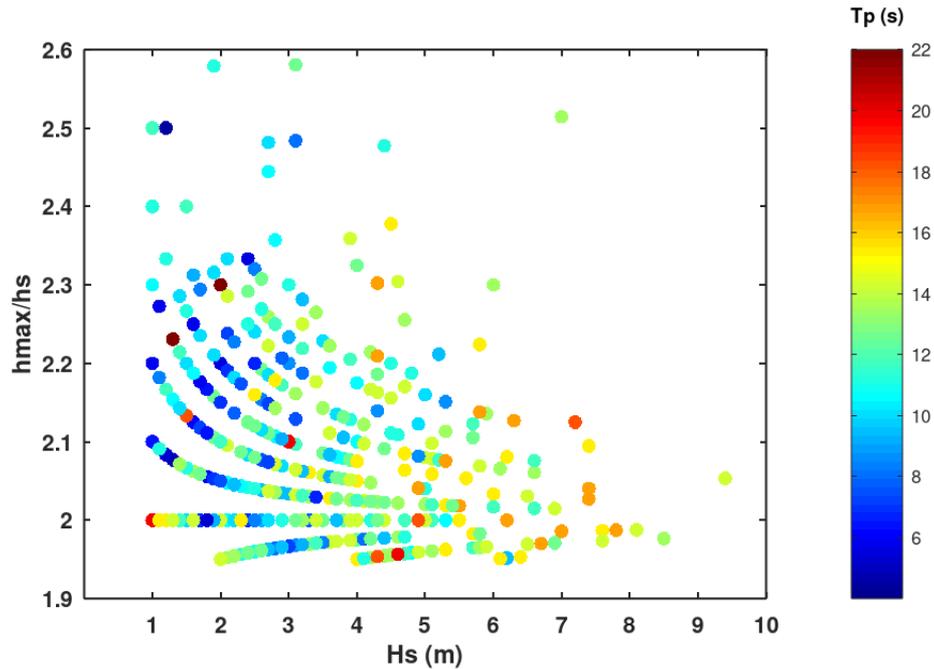
- No obvious relationship between SWIM spectral indexes and rogue waves observations at buoy
- We remind that there are few rogue waves observations and sometimes too far from buoy in a very variable field
- Spectral indexes from buoy or model may be more correlated with buoy (not studied).

Canary Islands (Atlantic)
2020/11/29 at 08:31





Conclusion



Statistics at 2 NE Atlantic buoys during 2 years